

Structured Perceptron

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Problem setup

- Restricted set of POS tags: adjective, preposition, verb, determiner, noun
- We first have sentence "time flies like an arrow" with true POS sequence NVPDN
- Features are $(z_i, z_{i+1}), (z_i, w_i)$
- What's a maximum violation POS sequence?

Problem setup

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- We first have sentence "time flies like an arrow" with true POS sequence NVPDN
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- What's a maximum violation POS sequence?
- Can do on paper because search is tractable

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- We first have sentence "time flies like an arrow" with true POS sequence NVPDN
- Features are $(z_i, z_{i+1}), (z_i, w_i)$
- What's a maximum violation POS sequence?
- Can do on paper because search is tractable
- So we're all on the same page, let's all use A A A A A

Correct answer: N V P D N

Prediction: A A A A A

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Correct answer: N V P D N

Prediction: A A A A A

Gold Features

(P, D) (N, arrow)

(D, an) (N, time)

(V, P) (P, like)

(V, flies) (START, N)

(D, N) (N, V)

Shared Features

Predicted Features

(A, arrow) (A, A)

(A, an) (A, like)

(START, A) (A, flies)

(A, time)

- Correct answer: N V P D N
- Prediction: A A A A A

(P, D) (N, arrow) (D, an) (N, time) (V, P) (P, like) (V, flies) (START, N)

(D, N) (N, V)

Shared Features

Predicted Features

(A, arrow) (A, A) (A, an) (A, like) (START, A) (A, flies) (A, time)

New feature vector: (A, A): -4.00; (A, an): -1.00; (A, arrow): -1.00; (A, flies): -1.00; (A, like): -1.00; (A, time): -1.00; (D, N): 1.00; (D, an): 1.00; (N, V): 1.00; (N, arrow): 1.00; (N, time): 1.00; (P, D): 1.00; (P, like): 1.00; (V, P): 1.00; (V, flies): 1.00; (START, A): -1.00; (START, N): 1.00

- Correct answer: N V P D N
- Prediction: A A A A A

(P, D) (N, arrow) (D, an) (N, time) (V, P) (P, like) (V, flies) (START, N) (D, N) (N, V)

Shared Features

Predicted Features

(A, arrow) (A, A) (A, an) (A, like) (START, A) (A, flies) (A, time)

```
New feature vector: (A, A): -4.00; (A, an): -1.00; (A, arrow): -1.00;
  (A, flies): -1.00; (A, like): -1.00; (A, time): -1.00; (D, N): 1.00;
  (D, an): 1.00; (N, V): 1.00; (N, arrow): 1.00; (N, time): 1.00; (P, D): 1.00;
  (P, like): 1.00; (V, P): 1.00; (V, flies): 1.00; (START, A): -1.00;
  (START, N): 1.00
```

fruit
$$_0$$
 flies $_1$ like $_2$ an $_3$ apple $_4$
$$\delta = V \\ D \\ N \end{pmatrix}$$
 (1)

$$w_{START, A} + w_{A, fruit} = -1.00 + 0.00 = -1.00$$

$$w_{\text{START, P}} + w_{\text{P, fruit}} = 0.00 + 0.00 = 0.00$$

$$\delta = V \begin{pmatrix} A \\ P \\ D \\ N \end{pmatrix} \begin{pmatrix} -1.00 \\ 0.00 \\ 0.00 \\ 0.00 \end{pmatrix}$$
 (1)

$$w_{START, V} + w_{V, fruit} = 0.00 + 0.00 = 0.00$$

$$\delta = V \begin{pmatrix} A \\ P \\ D \\ N \end{pmatrix} \begin{pmatrix} -1.00 \\ 0.00 \\ 0.00 \\ 0.00 \end{pmatrix} \tag{1}$$

$$w_{\text{START, D}} + w_{\text{D, fruit}} = 0.00 + 0.00 = 0.00$$

$$\delta = V \begin{pmatrix} 1.00 \\ 0.00 \\ 0.00 \\ 0.00 \\ 0.00 \\ 0.00 \end{pmatrix}$$
 (1)

$$w_{START. N} + w_{N. fruit} = 1.00 + 0.00 = 1.00$$

$$\delta_0(N) + w_{N, A} + w_{A, flies} = 1.00 + 0.00 + -1.00 = 0.00$$

$$\delta_0(N) + w_{N, P} + w_{P, flies} = 1.00 + 0.00 + 0.00 = 1.00$$

$$\delta_0(N) + w_{N, V} + w_{V, flies} = 1.00 + 1.00 + 1.00 = 3.00$$

$$\delta = V \left(\begin{array}{cccc} & \text{flies}_1 & \text{like}_2 & \text{an}_3 & \text{apple}_4 \\ A & -1.00 & 0.00 & \\ 0.00 & 1.00 & \\ 0.00 & 3.00 & \\ D & 0.00 & \\ N & 1.00 & \\ \end{array} \right)$$

$$\delta_0(P) + w_{P, D} + w_{D, flies} = 0.00 + 1.00 + 0.00 = 1.00$$

$$\delta = V \begin{pmatrix} F(1) & F(1) &$$

$$\delta_0(N) + w_{N, N} + w_{N, flies} = 1.00 + 0.00 + 0.00 = 1.00$$

$$\delta = V \begin{pmatrix} 1.00 & 1.00 & 1.00 \\ 0.00 & 1.00 & 0.00 \\ 0.00 & 1.00 & 0.00 \\ 0.00 & 1.00 & 0.00 \\ 0.00 & 1.00 & 0.00 \\ 1.00 & 1.00 & 0.00 \\ 0.00 & 1.00 & 0.00 \\ 1.00 & 1.00 & 0.00 \\ 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 \\$$

$$\delta_1(V) + w_{V, A} + w_{A, like} = 3.00 + 0.00 + -1.00 = 2.00$$

$$\delta = V \begin{pmatrix} f \text{ruit}_0 & \text{flies}_1 & \text{like}_2 & \text{an}_3 & \text{apple}_4 \\ -1.00 & 0.00 & 2.00 \\ 0.00 & 1.00 \\ 0.00 & 3.00 \\ 0.00 & 1.00 \\ 0.00 & 1.00 \\ 1.00 & 1.00 \end{pmatrix} \tag{1}$$

$$\delta_1(V) + w_{V.P} + w_{P.like} = 3.00 + 1.00 + 1.00 = 5.00$$

$$\delta = V \begin{pmatrix} fruit_0 & flies_1 & like_2 & an_3 & apple_4 \\ -1.00 & 0.00 & 2.00 \\ 0.00 & 1.00 & 5.00 \\ 0.00 & 3.00 \\ 0.00 & 1.00 \\ 1.00 & 1.00 \end{pmatrix} \tag{1}$$

$$\delta_1(V) + w_{V, V} + w_{V, like} = 3.00 + 0.00 + 0.00 = 3.00$$

$$\delta = V \begin{pmatrix} fruit_0 & flies_1 & like_2 & an_3 & apple_4 \\ -1.00 & 0.00 & 2.00 \\ 0.00 & 1.00 & 5.00 \\ 0.00 & 3.00 & 3.00 \\ 0.00 & 1.00 \\ 1.00 & 1.00 \end{pmatrix} \tag{1}$$

$$\delta_1(V) + w_{V.D} + w_{D.like} = 3.00 + 0.00 + 0.00 = 3.00$$

$$\delta = V \begin{pmatrix} fruit_0 & flies_1 & like_2 & an_3 & apple_4 \\ -1.00 & 0.00 & 2.00 \\ 0.00 & 1.00 & 5.00 \\ 0.00 & 3.00 & 3.00 \\ 0.00 & 1.00 & 3.00 \\ 1.00 & 1.00 & 0.00 \\ 0.00 & 1.00 & 0.00 \\ 0.00 & 1.00 & 0.00 \\ 0.00 & 1.00 & 0.00 \\ 0.00 & 1.00 & 0.00 \\ 0.00 & 0.00 & 0$$

$$\delta_1(V) + w_{V, N} + w_{N, like} = 3.00 + 0.00 + 0.00 = 3.00$$

$$\delta = V \begin{pmatrix} 1.00 &$$

$$\delta_2(P) + w_{P, A} + w_{A, an} = 5.00 + 0.00 + -1.00 = 4.00$$

$$\delta = V \left(\begin{array}{ccccc} & \text{fruit}_0 & \text{flies}_1 & \text{like}_2 & \text{an}_3 & \text{apple}_4 \\ & A & -1.00 & 0.00 & 2.00 & 4.00 \\ & D & 0.00 & 1.00 & 5.00 \\ & D & 0.00 & 3.00 & 3.00 \\ & D & 0.00 & 1.00 & 3.00 \\ & N & 1.00 & 1.00 & 3.00 \\ \end{array} \right)$$

$$\delta_2(P) + w_{P, P} + w_{P, an} = 5.00 + 0.00 + 0.00 = 5.00$$

$$\delta = V \begin{pmatrix} A \\ P \\ D \\ D \\ N \end{pmatrix} \begin{pmatrix} -1.00 & 0.00 & 2.00 & 4.00 \\ 0.00 & 1.00 & 5.00 & 5.00 \\ 0.00 & 3.00 & 3.00 \\ 0.00 & 1.00 & 3.00 \\ 1.00 & 1.00 & 3.00 \\ 0.00$$

$$\delta_2(P) + w_{P, V} + w_{V, an} = 5.00 + 0.00 + 0.00 = 5.00$$

$$\delta = V \begin{pmatrix} A \\ P \\ D \\ N \\ N \end{pmatrix} \begin{pmatrix} -1.00 & 0.00 & 2.00 & 4.00 \\ 0.00 & 1.00 & 5.00 & 5.00 \\ 0.00 & 3.00 & 3.00 & 5.00 \\ 0.00 & 1.00 & 3.00$$

$$\delta_2(P) + w_{P, D} + w_{D, an} = 5.00 + 1.00 + 1.00 = 7.00$$

$$\delta = V \begin{pmatrix} 1.00 &$$

$$\delta_2(P) + w_{P, N} + w_{N, an} = 5.00 + 0.00 + 0.00 = 5.00$$

$$\delta = V \left(\begin{array}{cccccc} & \text{fruit}_0 & \text{flies}_1 & \text{like}_2 & \text{an}_3 & \text{apple}_4 \\ A & -1.00 & 0.00 & 2.00 & 4.00 \\ 0.00 & 1.00 & 5.00 & 5.00 \\ 0.00 & 3.00 & 3.00 & 5.00 \\ D & 0.00 & 1.00 & 3.00 & 7.00 \\ N & 1.00 & 1.00 & 3.00 & 5.00 \\ \end{array} \right)$$

$$\delta_3(D) + w_{D, A} + w_{A, apple} = 7.00 + 0.00 + 0.00 = 7.00$$

$$\delta = V \begin{pmatrix} A \\ D \\ D \\ D \\ N \end{pmatrix} \begin{pmatrix} -1.00 & 0.00 & 2.00 & 4.00 & 7.00 \\ 0.00 & 1.00 & 5.00 & 5.00 \\ 0.00 & 3.00 & 3.00 & 5.00 \\ 0.00 & 1.00 & 3.00 & 7.00 \\ 0.00 & 1.00 & 3.00 & 5.00 \end{pmatrix} \tag{1}$$

$$\delta_3(D) + w_{D, P} + w_{P, apple} = 7.00 + 0.00 + 0.00 = 7.00$$

$$\delta = V \begin{pmatrix} Fruit_0 & flies_1 & like_2 & an_3 & apple_4 \\ -1.00 & 0.00 & 2.00 & 4.00 & 7.00 \\ 0.00 & 1.00 & 5.00 & 5.00 & 7.00 \\ 0.00 & 3.00 & 3.00 & 5.00 \\ D & 0.00 & 1.00 & 3.00 & 7.00 \\ N & 1.00 & 1.00 & 3.00 & 5.00 \end{pmatrix}$$
 (1)

$$\delta_3(D) + w_{D, V} + w_{V, apple} = 7.00 + 0.00 + 0.00 = 7.00$$

$$\delta = V \begin{pmatrix} F_1 & F_2 & F_3 & F_4 & F_$$

$$\delta_3(D) + w_{D, D} + w_{D, apple} = 7.00 + 0.00 + 0.00 = 7.00$$

$$\delta = V \begin{pmatrix} Fruit_0 & flies_1 & like_2 & an_3 & apple_4 \\ -1.00 & 0.00 & 2.00 & 4.00 & 7.00 \\ 0.00 & 1.00 & 5.00 & 5.00 & 7.00 \\ 0.00 & 3.00 & 3.00 & 5.00 & 7.00 \\ 0.00 & 1.00 & 3.00 & 7.00 & 7.00 \\ 0.00 & 1.00 & 3.00 & 5.00 \end{pmatrix}$$
 (1)

$$\delta_3(D) + w_{D, N} + w_{N, apple} = 7.00 + 1.00 + 0.00 = 8.00$$

Scores

$$\delta = V \begin{pmatrix} Fruit_0 & flies_1 & like_2 & an_3 & apple_4 \\ -1.00 & 0.00 & 2.00 & 4.00 & 7.00 \\ 0.00 & 1.00 & 5.00 & 5.00 & 7.00 \\ 0.00 & 3.00 & 3.00 & 5.00 & 7.00 \\ 0.00 & 1.00 & 3.00 & 7.00 & 7.00 \\ 0.00 & 1.00 & 3.00 & 5.00 & 8.00 \end{pmatrix}$$
(1)

Backpointers

(2)

Scores

$$\delta = V \begin{pmatrix} Fruit_0 & flies_1 & like_2 & an_3 & apple_4 \\ -1.00 & 0.00 & 2.00 & 4.00 & 7.00 \\ 0.00 & 1.00 & 5.00 & 5.00 & 7.00 \\ 0.00 & 3.00 & 3.00 & 5.00 & 7.00 \\ 0.00 & 1.00 & 3.00 & 7.00 & 7.00 \\ 0.00 & 1.00 & 3.00 & 5.00 & 8.00 \end{pmatrix}$$
 (1)

Backpointers

flies₁ like₂ an₃ apple₄

$$\beta = V$$

$$D$$

$$N$$

$$N$$

$$V$$

$$P$$

$$N$$

$$V$$

$$P$$

$$D$$

$$N$$

$$V$$

$$P$$

$$D$$

$$P$$

$$V$$

$$P$$

$$D$$

$$N$$

$$V$$

$$P$$

$$D$$

$$D$$

$$N$$

(2)

Scores

$$\delta = V \begin{pmatrix} f \text{files}_1 & \text{like}_2 & \text{an}_3 & \text{apple}_4 \\ -1.00 & 0.00 & 2.00 & 4.00 & 7.00 \\ 0.00 & 1.00 & 5.00 & 5.00 & 7.00 \\ 0.00 & 3.00 & 3.00 & 5.00 & 7.00 \\ D & 0.00 & 1.00 & 3.00 & 7.00 & 7.00 \\ N & 1.00 & 1.00 & 3.00 & 5.00 & 8.00 \end{pmatrix}$$
 (1)

Backpointers

flies₁ like₂ an₃ apple₄

A
$$\begin{pmatrix} N & V & P & D \\ P & N & V & P & D \\ N & V & P & D \\ D & N & V & P & D \\ N & V & P & D \\ N & V & P & D \end{pmatrix}$$
(2)

Reconstruction: N V P D N

- Old feature vector: (A, A): -4.00; (A, an): -1.00; (A, arrow): -1.00; (A, flies): -1.00; (A, like): -1.00; (A, time): -1.00; (D, N): 1.00; (D, an): 1.00; (N, V): 1.00; (N, arrow): 1.00; (N, time): 1.00; (P, D): 1.00; (P, like): 1.00; (V, P): 1.00; (V, flies): 1.00; (START, A): -1.00; (START, N): 1.00
- Correct answer: A N V D N
- Prediction: N V P D N

- Old feature vector: (A, A): -4.00; (A, an): -1.00; (A, arrow): -1.00; (A, flies): -1.00; (A, like): -1.00; (A, time): -1.00; (D, N): 1.00; (D, an): 1.00; (N, V): 1.00; (N, arrow): 1.00; (N, time): 1.00; (P, D): 1.00; (P, like): 1.00; (V, P): 1.00; (V, flies): 1.00; (START, A): -1.00; (START, N): 1.00
- Correct answer: A N V D N
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- Old feature vector: (A, A): -4.00; (A, an): -1.00; (A, arrow): -1.00; (A, flies): -1.00; (A, like): -1.00; (A, time): -1.00; (D, N): 1.00; (D, an): 1.00; (N, V): 1.00; (N, arrow): 1.00; (N, time): 1.00; (P, D): 1.00; (P, like): 1.00; (V, P): 1.00; (V, flies): 1.00; (START, A): -1.00; (START, N): 1.00
- Correct answer: A N V D N
- Prediction: N V P D N

(V, D) (A, N) (A, fruit) (V, like) (START, A) (N, flies)

Shared Features

(D, an) (N, V) (N, apple) (D, N)

Predicted Features

(P, D) (V, P) (P, like) (V, flies) (START, N) (N, fruit)

- Old feature vector: (A, A): -4.00; (A, an): -1.00; (A, arrow): -1.00; (A, flies): -1.00; (A, like): -1.00; (A, time): -1.00; (D, N): 1.00; (D, an): 1.00; (N, V): 1.00; (N, arrow): 1.00; (N, time): 1.00; (P, D): 1.00; (P, like): 1.00; (V, P): 1.00; (V, flies): 1.00; (START, A): -1.00; (START, N): 1.00
- Correct answer: A N V D N
- Prediction: N V P D N

(V, D) (A, N) (A, fruit) (V, like) (START, A) (N, flies)

Shared Features

(D, an) (N, V) (N, apple) (D, N)

Predicted Features

(P, D) (V, P) (P, like) (V, flies) (START, N) (N, fruit)

New feature vector: (A, A): -4.00; (A, N): 1.00; (A, an): -1.00; (A, arrow): -1.00; (A, flies): -1.00; (A, fruit): 1.00; (A, like): -1.00; (A, time): -1.00; (D, N): 1.00; (D, an): 1.00; (N, V): 1.00; (N, arrow): 1.00; (N, flies): 1.00; (N, fruit): -1.00; (N, time): 1.00; (V, D): 1.00; (V, like): 1.00; (P, D): 0.00;

- Old feature vector: (A, A): -4.00; (A, an): -1.00; (A, arrow): -1.00; (A, flies): -1.00; (A, like): -1.00; (A, time): -1.00; (D, N): 1.00; (D, an): 1.00; (N, V): 1.00; (N, arrow): 1.00; (N, time): 1.00; (P, D): 1.00; (P, like): 1.00; (V, P): 1.00; (V, flies): 1.00; (START, A): -1.00; (START, N): 1.00
- Correct answer: A N V D N
- Prediction: N V P D N

(V, D) (A, N) (A, fruit) (V, like) (START, A) (N, flies)

Shared Features

(D, an) (N, V) (N, apple) (D, N)

Predicted Features

(P, D) (V, P) (P, like) (V, flies) (START, N) (N, fruit)

New feature vector: (A, A): -4.00; (A, N): 1.00; (A, an): -1.00; (A, arrow): -1.00; (A, flies): -1.00; (A, fruit): 1.00; (A, like): -1.00; (A, time): -1.00; (D, N): 1.00; (D, an): 1.00; (N, V): 1.00; (N, arrow): 1.00; (N, flies): 1.00; (N, fruit): -1.00; (N, time): 1.00; (V, D): 1.00; (V, like): 1.00; (P, D): 0.00;

Wrapup

- Not just for POS tagging: parsing, machine translation
- Hard to overstate how important features $\vec{\Phi}$ are
- Next time: can we get algorithm to find features for us?

Wrapup

- Not just for POS tagging: parsing, machine translation
- Hard to overstate how important features $\vec{\Phi}$ are
- Next time: can we get algorithm to find features for us?
- Project ideas:
 - Deep learning of features
 - Applying perceptron to your favorite problem, designing great features
 - Efficient data structures for finding max violation