Algorithm: Active Learning with Topic Overviews for Speeding Label Induction and Document Labeling

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Abstract

Effective text classification requires experts to annotate data with labels; these training data are time-consuming and expensive to obtain. If you know what labels you want, active learning can reduce the number of labeled documents needed. However, establishing the label set remains difficult. Annotators often lack the global knowledge needed to induce a label set. We introduce ALTO: Active Learning with Topic Overviews, an interactive system to help humans annotate documents: topic models provide a global overview of what labels to create and active learning directs them to the right documents to label. Our forty-annotator user study shows that while active learning alone is best in extremely resource limited conditions, topic models (even by themselves) lead to better label sets, and ALTO’s combination is best overall.

1 Introduction

Many fields depend on texts labeled by human experts; computational linguistics uses such annotation to determine word senses and sentiment (Kelly and Stone, 1975; Kim and Hovy, 2004); while social science uses “coding” to scale up and systematize content analysis (Budge, 2001; Klingemann et al., 2006).

Classification takes these labeled data as a training set and labels new data automatically. Creating a broadly applicable and consistent label set that generalizes well is time-consuming and difficult, requiring expensive annotators to examine large swaths of the data. Effective NLP systems must measure (Hwa, 2004; Osborne and Baldridge, 2004; Ngai and Yarowsky, 2000) and reduce annotation cost (Tomanek et al., 2007). Annotation is hard because it requires both global and local knowledge of the entire dataset. Global knowledge is required to create the set of labels, and local knowledge is required to annotate the most useful examples to serve as a training set for an automatic classifier. The former’s cost is often hidden in multiple rounds of refining annotation guidelines.

We create a single interface—ALTO (Active Learning with Topic Overviews)—to address both global and local challenges using two machine learning tools: topic models and active learning (we review both in Section 2). Topic models address the need for annotators to have a global overview of the data, exposing the broad themes of the corpus so annotators know what labels to create. Active learning selects documents that help the classifier understand the differences between labels and directs the user’s attention locally to them. We provide users four experimental conditions to compare the usefulness of a topic model or a simple list of documents, with or without active learning suggestions (Section 3). We then describe our data and evaluation metrics (Section 4).

Through both synthetic experiments (Section 5) and a user study (Section 6) with forty participants, we evaluate ALTO and its constituent components by comparing results from the four conditions introduced above. We first examine user strategies for organizing documents, user satisfaction, and user efficiency. Finally, we evaluate the overall effectiveness of the label set in a post study crowdsourced task.
Table 1: Given a dataset—in this case, the US congressional bills dataset—topics are automatically discovered sorted lists of terms that summarize segments of a document collection. Topics also are associated with documents. These topics give users a sense of documents’ main themes and help users create high-quality labels.

2 Topic Overviews and Active Learning

ALTO, a framework for assigning labels to documents that uses both global and local knowledge to help users create and assign document labels, has two main components: topic overview and active learning selection. We explain how ALTO uses topic models and active learning to aid label induction and document labeling.

**Topic Models** Topic models (Blei et al., 2003) automatically induce structure from a text corpus. Given a corpus and a constant K for the number of topics, topic models output (i) a distribution over words for each topic k (φ_k,w) and (ii) a distribution over topics for each document (θ_d,k). Each topic’s most probable words and associated documents can help a user understand what the collection is about. Table 1 shows examples of topics and their highest associated documents from our corpus of US congressional bills.

Our hypothesis is that showing documents grouped by topics will be more effective than having the user wade through an undifferentiated list of random documents and mentally sort the major themes themselves.

**Active Learning** Active learning (Settles, 2012) directs users’ attention to the examples that would be most useful to label when training a classifier. When user time is scarce, active learning builds a more effective training set than random labeling: uncertainty sampling (Lewis and Gale, 1994) or query by committee (Seung et al., 1992) direct users to the most useful documents to label.

In contrast to topic models, active learning provides local information: *this document* is the one you should pay attention to. Our hypothesis is that active learning directing users to documents most beneficial to label will not only be more effective than randomly selecting documents but will also complement the global information provided by topic models. Section 3.3 describes our approaches for directing user’s local attention.

3 Study Conditions

Our goal is to characterize how local and global knowledge can aid users in annotating a dataset. This section describes our four experimental conditions and outlines the user’s process for labeling documents.

3.1 Study Design

The study uses a 2 × 2 between-subjects design, with factors of document collection overview (two levels: topic model or list) and document selection (two levels: active or random). The four conditions, with the TA condition representing ALTO, are:

1. Topic model overview, active selection (TA)
2. Topic model overview, random selection (TR)
3. List overview, active selection (LA)
4. List overview, random selection (LR)

3.2 Document Collection Overview

The topic and list overviews offer different overall structure but the same basic elements for users to create, modify, and apply labels (Section 3.4). The topic overview (Figure 1a) builds on Hu et al. (2014): for each topic, the top twenty words are shown alongside twenty document titles. Topic words (w) are sized based on their probability φ_k,w in the topic k and the documents with the highest probability of that topic (θ_d,k) are shown. The list overview, in contrast, presents documents as a simple, randomly ordered list of titles (Figure 1b). We display the same number of documents (20K, where K is the total number of topics) in both the topic model and list overviews, but the list overview provides no topic information.

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3.3 Document Selection

We use a preference function $U$ to direct users’ attention to specific documents. To provide consistency across the four conditions, each condition will highlight the document that scores the highest for the condition’s preference function. For the random selection conditions, TR and LR, document selection is random, within a topic or globally. We expect this to be less useful than active learning. The document preference functions are:

**LA**:

La uses traditional uncertainty sampling:

$$U_{d}^{LA} = H_{C} [Y_{d}],$$

where $H_{C} [Y_{d}] = - \sum_{i} P(y_{i}|d) \log P(y_{i}|d)$ is the classifier entropy. Entropy measures how confused (uncertain) classifier $C$ is about its prediction of a document $d$’s label $y$. Intuitively, it prefers documents the classifier suggests many labels instead of a single, confident prediction.

**LR**:

LR’s approach is the same as LA’s except we replace $H_{C} [Y_{d}]$ with a uniform random number:

$$U_{d}^{LR} \sim \text{unif}(0, 1).$$

In contrast to LA, which suggests the most uncertain document, LR suggests a random document.
Dasgupta and Hsu (2008) argue that clustering should inform active learning criteria, balancing coverage against classifier accuracy. We adapt their method to flat topic models—in contrast to their hierarchical cluster trees—by creating a composite measure of document uncertainty within a topic:

\[ U_d^{TA} = \mathbb{H}_C [y_d] \theta_{d,k}, \]  

(3)

where \( k \) is the prominent topic for document \( d \). \( U_d^{TA} \) prefers documents that are representative of a topic (i.e., have a high value of \( \theta_{d,k} \) for that topic) and are informative for the classifier.

**TA**: TA’s approach is the same as LA’s except we replace \( \mathbb{H}_C [y_d] \) with a uniformly random number:

\[ U_d^{TR} = \text{unif}(0, 1) \theta_{d,k}. \]  

(4)

Similar to TA, \( U_d^{TR} \) prefers documents that are representative of a topic, but not any particular document in the topic. Incorporating the random component encourages covering different documents in diverse topics.

In LA and LR, the preference function directly chooses a document and directs the user to it. On the other hand, \( U_d^{TA} \) and \( U_d^{TR} \) are topic dependent. TA emphasizes documents that are both informative to the classifier and representative of a topic; if a document is not representative, the surrounding context of a topic will be less useful. Therefore, the factor \( \theta_{d,k} \) appears in both. Thus, they require that a topic be chosen first and then the document with maximum preference, \( U \), within that topic can be chosen. In TR, the topic is chosen randomly. In TA, the topic is chosen by

\[ k^* = \arg \max_k (\text{median}_d(\mathbb{H}_C [y_d] \theta_{d,k})). \]  

(5)

That is the topic with the maximum median \( U \). Median encodes how “confusing” a topic is. In other words, topic \( k^* \) is the topic that its documents confuse the classifier most.

### 3.4 User Labeling Process

The user’s labeling process is the same in all four conditions. The *overview* (topic or list) allows users to examine individual documents (Figure 1). Clicking on a document opens a dialog box (Figure 2) with the text of the document and three options:

1. Create and assign a new label to the document.
2. Choose an existing label for the document.
3. Skip the document.

Once the user has labeled two documents with different labels, the displayed documents are replaced based on the preference function (Section 3.3), every time the user labels (or updates labels for) a document. In TA and TR, each topic’s documents are replaced with the twenty highest ranked documents. In LA and LR, all documents are updated with the top \( 20K \) ranked documents.

The system also suggests one document to consider by auto-scrolling to it and drawing a red box around its title (Figure 3). The user may ignore that document and click on any other document. After the user labels ten documents, the classifier runs and assigns labels to other documents. For classifier-labeled documents, the user can either approve the label or assign a different label. The process continues until the user is satisfied or a time runs out (forty minutes in our user study, Section 6). We use time to control for the varying difficulty of assigning document labels: active learning will select more difficult documents to annotate, but they may be more useful; time is a more fair basis of comparison in real-world tasks.

### 4 Data and Evaluation Metrics

In this section, we describe our data, the machine learning techniques to learn classifiers from examples, and the evaluation metrics to know whether the final labeling of the complete documents collection was successful.

#### 4.1 Datasets

**Data** Our experiments require corpora to compare user labels with gold standard labels. We experiment with two corpora: 20Newsgroups (Lang, 2007) and US congressional bills from GovTrack.

For US congressional bills, GovTrack provides bill information such as the title and text, while the Congressional Bills Project (Adler and Wilkerson, 2006) provides labels and sub-labels for the bills. Examples of labels are agriculture and health, while sub-labels include agricultural trade and comprehensive health care reform.

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1 Outliers skew other measures (e.g., max or mean).

2 In all conditions, the number of displayed unlabeled documents is adjusted based on the number of manually labeled documents. i.e. if the user has labeled \( n \) documents in topic \( k \), \( n \) manually labeled documents followed by top \( 20 - n \) uncertain documents will be shown in topic \( k \).

3 To reduce user confusion, for each existing label, only the top 100 documents get a label assigned in the UI.

4 https://www.govtrack.us/
top-level labels have been developed by consensus over many years by a team of top political scientists to create a reliable, robust dataset. We use the 112th Congress; after filtering, this dataset has 5558 documents. We use this dataset in both the synthetic experiments (Section 5) and the user study (Section 6).

The 20 Newsgroups corpus has 19,997 documents grouped in twenty news groups that are further grouped into six more general topics. Examples are talk.politics.guns and sci.electronics, which belong to the general topics of politics and science. We use this dataset in synthetic experiments (Section 5).

4.2 Machine Learning Techniques

Topic Modeling To choose the number of topics ($K$), we calculate average topic coherence (Lau et al., 2014) on US Congressional Bills, between ten and forty topics and choose $K = 19$, as it has the maximum coherence score. For consistency, we use the same number of topics ($K = 19$) for 20 Newsgroups corpus. After filtering words based on TF-IDF, we use Mallet (McCallum, 2002) with default options to learn topics.

Features and Classification A logistic regression predicts labels for documents and provides the classification uncertainty for active learning. To make classification and active learning updates efficient, we use incremental learning (Carpenter, 2008, LingPipe). We update classification parameters using stochastic gradient descent, restarting with the previously learned parameters as new labeled documents become available. We use cross validation, using argmax topics as surrogate labels, to set the parameters for learning the classifier.

The features for classification include topic probabilities, unigrams, and the fraction of labeled documents in each document’s prominent topic. The intuition behind adding this last feature is to allow active learning to suggest documents in a diverse range of topics if it finds this feature a useful indicator of uncertainty.

4.3 Evaluation Metrics

Our goal is to create a system that allows users to quickly induce a high-quality label set. We compare the user-created label sets against the data’s gold label sets. Comparing different clusterings is a difficult task, so we use three clustering evaluation metrics: purity (Zhao and Karypis, 2001), rand index (Rand, 1971, RI), and normalized mutual information (Strehl and Ghosh, 2003, NMI).

Purity The documents labeled with a good user label should only have one (or a few) gold labels associated with them: this is measured by cluster purity. Given each user cluster, it measures what fraction of the documents in a user cluster belong to the most frequent gold label in that cluster:

$$\text{purity}(\Omega, G) = \frac{1}{N} \sum_l \max_j |\Omega_l \cap G_j|,$$

where $L$ is the number of labels user creates, $\Omega = \{\Omega_1, \Omega_2, \ldots, \Omega_L\}$ is the user clustering of documents, $G = \{G_1, G_2, \ldots, G_J\}$ is gold clustering of documents, and $N$ is the total number of documents. The user $\Omega_l$ and gold $G_j$ labels are interpreted as sets containing all documents assigned to that label.

Rand index (RI) RI is a pair counting measure, where cluster evaluation is considered as a series of decisions. If two documents have the same gold label and the same user label (TP) or if they do not have the same gold label and are not assigned the same user label (TN), the decision is right. Otherwise, it is wrong (FP, FN). RI measures the percentage of decisions that are right:

$$\text{RI} = \frac{TP + TN}{TP + FP + TN + FN}.$$  

Normalized mutual information (NMI) NMI is an information theoretic measure that measures the amount of information one gets about the gold clusters by knowing what the user clusters are:
where $\Omega$ and $G$ are user and gold clusters, $H$ is the entropy and $I$ is mutual information (Bouma, 2009).

While purity, $R_1$, and $NMI$ are all normalized within $[0, 1]$ (higher is better), they measure different things. Purity measures the intersection between two clusterings, it is sensitive to the number of clusters, and it is not symmetric.

On the other hand, $R_1$ and $NMI$ are less sensitive to the number of clusters and are symmetric. $R_1$ measures pairwise agreement in contrast to purity’s emphasis on intersection. Moreover, $NMI$ measures shared information between two clusterings.

None of these metrics are perfect: purity can be exploited by putting each document in its own label, $R_1$ does not distinguish separating similar documents with distinct labels from giving dissimilar documents the same label, and $NMI$’s ability to compare different numbers of clusters means that it sometimes gives high scores for clusterings by chance. Given the diverse nature of these metrics, if a labeling does well in all three of them, we can be relatively confident that it is not a degenerate solution that games the system.

5 Synthetic Experiments

Before running a user study, we test our hypothesis that topic model overviews and active learning selection improve final cluster quality compared to standard baselines: list overview and random selection. We simulate the four conditions on Congressional Bills and 20 Newsgroups.

Since we believe annotators create more specific labels compared to the gold labels, we use sublabels as simulated user labels and labels as gold labels (we give examples of labels and sub-labels in Section 4.1). We start with two randomly selected documents that have different sub-labels, assign the corresponding sub-labels, then add more labels based on each condition’s preference function (Section 3.3). We follow the condition’s preference function and incrementally add labels until 100 documents have been labeled (100 documents are representative of what a human can label in about an hour). Given these labels, we compute purity, $R_1$, and $NMI$ over time. This procedure is repeated fifteen times (to account for the randomness of initial document selections and the preference functions with randomness).

Synthetic results validate our hypothesis that topic overview and active learning selection can help label a corpus more efficiently (Figure 4). $LA$ shows early gains, but tends to falter eventually compared to both topic overview and topic overview combined with active learning selection ($TR$ and $TA$).

However, these experiments do not validate ALTO. Not all documents require the same time or effort to label, and active learning focuses on the hardest examples, which may confuse users. Thus, we need to evaluate how effectively actual users annotate a collection’s documents.

6 User Study

Following the synthetic experiments, we conduct a user study with forty participants to evaluate ALTO (TA condition) against three alternatives that lack topic overview ($LA$), active learning selection ($TR$), or both ($LR$) (Sections 6.1 and 6.2). Then, we conduct a crowdsourced study to compare the overall

effectiveness of the label set generated by the participants in the four conditions (Section 6.3).

6.1 Method

We use the freelance marketplace Upwork to recruit online participants. We require participants to have more than 90% job success on Upwork, English fluency, and US residency. Participants are randomly assigned to one of the four conditions and we recruited ten participants per condition.

Participants completed a demographic questionnaire, viewed a video of task instructions, and then interacted with the system and labeled documents until satisfied with the labels or forty minutes had elapsed. The session ended with a survey, where participants rated mental, physical, and temporal demand, and performance, effort, and frustration on 20-point scales, using questions adapted from the NASA Task Load Index (Hart and Staveland, 1988, TLX). The survey also included 7-point scales for ease of coming up with labels, usefulness and satisfaction with the system, and—for TR and LA—topic information helpfulness. Each participant was paid fifteen dollars.

For statistical analysis, we primarily use $2 \times 2$ (overview $\times$ selection) ANOVAs with Aligned Rank Transform (Wobbrock et al., 2011, ART), which is a non-parametric alternative to a standard ANOVA that is appropriate when data are not expected to meet the normality assumption of ANOVA.

6.2 Document Cluster Evaluation

We analyze the data by dividing the forty-minute labeling task into five minute intervals. If a participant stops before the time limit, we consider their final dataset to stay the same for any remaining intervals. Figure 5 shows the measures across study conditions, with similar trends for all three measures.

Table 2: Results from $2 \times 2$ ANOVA with ART analyses on the final purity, R1, and NMI metrics. Only main effects for the factors of overview and selection are shown; no interaction effects were statistically significant. Topics and active learning both had significant effects on quality scores.

<table>
<thead>
<tr>
<th></th>
<th>Overview</th>
<th>Selection</th>
<th>Overview</th>
<th>Selection</th>
</tr>
</thead>
<tbody>
<tr>
<td>final purity</td>
<td>81.03</td>
<td>7.18</td>
<td>&lt; .001</td>
<td>.011</td>
</tr>
<tr>
<td>final R1</td>
<td>39.89</td>
<td>6.28</td>
<td>&lt; .001</td>
<td>.017</td>
</tr>
<tr>
<td>final NMI</td>
<td>70.92</td>
<td>9.87</td>
<td>&lt; .001</td>
<td>.003</td>
</tr>
</tbody>
</table>

Table 2: Results from $2 \times 2$ ANOVA with ART analyses on the final purity, R1, and NMI metrics. Only main effects for the factors of overview and selection are shown; no interaction effects were statistically significant. Topics and active learning both had significant effects on quality scores.

TR outperforms LA. Topic models by themselves outperform traditional active learning strategies (Figure 5). LA performs better than LR; while active learning was useful, it was not as useful as the topic model overview (TR and TA).

LA provides an initial benefit. Average purity, NMI and R1 were highest with LA for the earliest labeling time intervals. Thus, when time is very

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Figure 5: User study results on US Congressional Bills dataset. Active learning selection helps initially, but the combination of active learning selection and topic model overview has highest quality labels by the end of the task.
Table 3: Mean, standard deviation, and median purity, RI, and NMI after ten minutes. NMI in particular shows the benefit of LA over other conditions at early time intervals.

<table>
<thead>
<tr>
<th></th>
<th>purity</th>
<th>RI</th>
<th>NMI</th>
</tr>
</thead>
<tbody>
<tr>
<td>TA</td>
<td>0.31 ± 0.08 [0.32]</td>
<td>0.80 ± 0.05 [0.80]</td>
<td>0.19 ± 0.08 [0.21]</td>
</tr>
<tr>
<td>TR</td>
<td>0.32 ± 0.09 [0.31]</td>
<td>0.82 ± 0.04 [0.82]</td>
<td>0.21 ± 0.09 [0.20]</td>
</tr>
<tr>
<td>LR</td>
<td>0.31 ± 0.04 [0.31]</td>
<td>0.79 ± 0.04 [0.79]</td>
<td>0.19 ± 0.03 [0.19]</td>
</tr>
</tbody>
</table>

6.3 Label Evaluation Results

Section 6.2 compares clusters of documents in different conditions against the gold clusters but does not evaluate the quality of the labels themselves. Since one of the main contributions of ALTO is to accelerate inducing a high quality label set, we use crowdsourcing to assess how the final induced label sets compare in different conditions.

For completeness, we also compare labels against a fully automatic labeling method (Aletras and Stevenson, 2014) that does not require human intervention. We assign automatic labels to documents based on their most prominent topic.

We ask users on a crowdsourcing platform to vote for the “best” and “worst” label that describes the content of a US congressional bill (we use Crowdflower restricted to US contributors).

Five users label each document and we use the aggregated results generated by Crowdflower. The user gets $0.20 for each task.

We randomly choose 200 documents from our dataset (Section 4.1). For each chosen document, we randomly choose a participant from all four conditions (TA, TR, LA, LR). The labels assigned in different conditions and the automatic label of the document’s prominent topic construct the candidate labels for the document. Identical labels are merged into one label to avoid showing duplicate labels to users. If a merged label gets a “best” or “worst” vote, we split that vote across all the identical instances.

Figure 6 shows the average number of “best” and “worst” votes for each condition and the automatic method. ALTO (TA) receives the most “best” votes and the fewest “worst” votes. LR receives the most worst votes. The automatic labels, interestingly, appear to do at least as well as the list view labels, with a similar number of best votes and fewer worst votes. This indicates that automatic labels have reasonable quality compared to at least some manually generated labels. However, when users are provided with a topic model overview—

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Some participants had typos in the labels. We corrected all the typos using pyEnchant (http://pythonhosted.org/pyenchant/) spellchecker. If the corrected label was still wrong, we corrected it manually.

with or without active learning selection—they can generate label sets that improve upon automatic labels and labels assigned without the topic model overview.

7 Related Work

Text classification—a ubiquitous machine learning tool for automatically labeling text (Zhang, 2010)—is a well-trodden area of NLP research. The difficulty is often creating the training data (Hwa, 2004; Osborne and Baldrige, 2004); coding theory is an entire subfield of social science devoted to creating, formulating, and applying labels to text data (Saldana, 2012; Musialek et al., 2016). Crowdsourcing (Snow et al., 2008) and active learning (Settles, 2012), can decrease the cost of annotation but only after a label set exists.

ALTO’s corpus overview aid text understanding, building on traditional interfaces for gaining both local and global information (Hearst and Pedersen, 1996). More elaborate interfaces (Eisenstein et al., 2012; Chaney and Blei, 2012; Roberts et al., 2014) provide richer information given a fixed topic model. Alternatively, because topic models are imperfect (Boyd-Graber et al., 2014), refining underlying topic models may also improve users’ understanding of a corpus (Choo et al., 2013; Hoque and Carenini, 2015).

Summarizing document collections through discovered topics can happen through raw topics labeled manually by users (Talley et al., 2011), automatically (Lau et al., 2011), or by learning a mapping from labels to topics (Ramage et al., 2009). When there is not a direct correspondence between topics and labels, classifiers learn a mapping (Blei and McAuliffe, 2007; Zhu et al., 2009; Nguyen et al., 2015). Because we want topics to be consistent between users, we use a classifier with static topics in ALTO. Combining our interface with dynamic topics could improve overall labeling, perhaps at the cost of introducing confusion as topics change during the labeling process.

8 Conclusion and Future Work

We introduce ALTO, an interactive framework that combines both active learning selections with topic model overviews to both help users induce a label set and assign labels to documents. We show that users can more effectively and efficiently induce a label set and create training data using ALTO in comparison with other conditions, which lack either topic overview or active selection.

We can further improve ALTO to help users gain better and faster understanding of text corpora. Our current system limits users to view only 20K documents at a time and allows for one label assignment per document. Moreover, the topics are static and do not adapt to better reflect users’ labels. Users should have better support for browsing documents and assigning multiple labels.

Finally, with slight changes to what the system considers a document, we believe ALTO can be extended to NLP applications other than classification, such as named entity recognition or semantic role labeling, to reduce the annotation effort.

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<table>
<thead>
<tr>
<th>Condition</th>
<th>Mental Demand</th>
<th>Physical Demand</th>
<th>Temporal Demand</th>
<th>Performance</th>
<th>Effort</th>
<th>Frustration</th>
</tr>
</thead>
</table>

Table 4: Mean, standard deviation, and median results from NASA-TLX post-survey. All questions are scaled 1 (low)–20 (high), except performance, which is scaled 1 (good)–20 (poor). Users found topic model overview conditions, TR and TA, to be significantly less frustrating than the list overview conditions.
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